

## COMMUTATIVITY OF PRIME RINGS WITH SYMMETRIC BIDERIVATIONS

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### Abstract

The present paper shows some results on the commutativity of  $R$ : Let  $R$  be a prime ring and for any nonzero ideal  $I$  of  $R$ , if  $R$  admits a biderivation  $B$  such that it satisfies any one of the following properties (i)  $B([x, y], z) = [x, y]$ , (ii)  $B([x, y], m) + [x, y] = 0$ , (iii)  $B(xoy, z) = xoy$ , (iv)  $B(xoy, z) + xoy = 0$ , (v)  $B(x, y)oB(y, z) = 0$ , (vi)  $B(x, y)oB(y, z) = xoz$ , (vii)  $B(x, y)oB(y, z) + xoy = 0$ , for all  $x, y, z \in R$ , then  $R$  is a commutative ring.

**Keywords:** prime ring, biderivation, commutativity and ideals.

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