

## NONDISTRIBUTIVE RINGS AND THEIR ÖRE LOCALIZATIONS

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### Abstract

In the paper, we introduce the notion of a nondistributive ring  $N$  as a generalization of the notion of an associative ring with unit, in which the addition needs not be abelian and the distributive law is replaced by  $n0 = 0n = 0$  for every element  $n$  of  $N$ . For a nondistributive ring  $N$ , we introduce the notion of a nondistributive ring of left quotients  $S^{-1}N$  with respect to a multiplicatively closed set  $S \subseteq N$ , and determine necessary and sufficient conditions for the existence of  $S^{-1}N$ .

**Keywords:** semigroups, nearrings, nondistributive rings, nearrings of quotients, nondistributive rings of quotients, Öre localizations of nondistributive rings.

**2010 Mathematics Subject Classification:** 16Y99, 16Y30, 12K05, 16S85, 16U20.

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Received 10 October 2016

Revised 13 July 2017

Accepted 20 May 2018