

TRACE INEQUALITIES FOR POSITIVE SEMIDEFINITE MATRICES

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AND

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Abstract

Certain trace inequalities for positive definite matrices are generalized for positive semidefinite matrices using the notion of the group generalized inverse.

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