

## ALL MAXIMAL COMPLETELY REGULAR SUBMONOIDS OF $Hyp_G(2)$

PORNPIMOL KUNAMA

AND

SORASAK LEERATANAVALEE<sup>1</sup>

*Department of Mathematics  
Faculty of Science, Chiang Mai University  
Chiang Mai 50200, Thailand*

e-mail: pornpimol5331@gmail.com  
sorasak.l@cmu.ac.th

### Abstract

In this paper we consider mappings  $\sigma$  which map the binary operation symbol  $f$  to the term  $\sigma(f)$  which do not necessarily preserve the arity. These mapping are called generalized hypersubstitutions of type  $\tau = (2)$  and we denote the set of all these generalized hypersubstitutions of type  $\tau = (2)$  by  $Hyp_G(2)$ . The set  $Hyp_G(2)$  together with a binary operation defined on this set and the identity generalized hypersubstitution which maps  $f$  to the term  $f(x_1, x_2)$  forms a monoid. In this paper, we determine all maximal completely regular submonoids of this monoid.

**Keywords:** generalized hypersubstitution, regular element, completely regular.

**2010 Mathematics Subject Classification:** 20M07, 08B15, 08B25.

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<sup>1</sup>Corresponding author.

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Received 29 March 2017

Revised 2 April 2017