

***M*-SOLID GENERALIZED NON-DETERMINISTIC VARIETIES**

SOMSAK LEKKOKSUNG

Department of Mathematics, Faculty of Engineering
Rajamangala University of Technology Isan
Khon Kaen Campus. 40000, Thailand

e-mail: lekkoksung_somsak@hotmail.com

Abstract

A generalized non-deterministic hypersubstitution is a mapping which maps operation symbols of type τ to the set of terms of the same type which does not necessarily preserve the arity. We apply the generalized non-deterministic hypersubstitution to an algebra of type τ and obtain a class of derived algebras of type τ . The generalized non-deterministic hypersubstitutions can be also applied to sets of equations of type τ . We obtain two closure operators which turn out to be a conjugate pair of completely additive closure operators. This allows us to apply the theory of conjugate pairs of additive closure operators to characterize *M*-solid generalized non-deterministic varieties of algebras.

Keywords: generalized non-deterministic hypersubstitution, conjugate pair of additive closure operators, *M*-solid generalized non-deterministic variety.

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