

ENUMERATION OF Γ -GROUPS OF FINITE ORDER

DARIUSH HEIDARI

*Faculty of Science
Mahallat institute of higher education
Mahallat, Iran*

e-mail: dheidari82@gmail.com

AND

MARZIEH AMOOSHAHI

*Faculty of Science
Mahallat institute of higher education
Mahallat, Iran*

e-mail: mz.amooshahi@gmail.com

Abstract

The concept of Γ -semigroups is a generalization of semigroups. In this paper, we consider Γ -groups and prove that every Γ -group is derived from a group then, we give the number of Γ -groups of small order.

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